



**PDHonline Course K154 (4 PDH)**

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# **Practical Multi-Factor Test Design and Analysis**

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**PDH Online | PDH Center**

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## Practical Multi-Factor Test and Analysis

### Quiz Questions

1. Multi-Factor testing can identify interactions between controlled factors.
  - a. True
  - b. False
2. Equipment specifications are not an important consideration in test design.
  - a. True
  - b. False
3. Uncontrolled factors like weather conditions can be ignored.
  - a. True
  - b. False
4. The variance of a population is

$$\sigma^2 = \frac{\sum_{n=1}^N (S_n - \mu)^2}{(N-1)}$$

- a. True
  - b. False
5. The Sample Standard Deviation is the square root of the Sample Variance.
  - a. True
  - b. False
6. In a normally distributed population, what percentage will be within 1 standard deviation of the mean?
  - a. 95.4 %
  - b. 50.2 %
  - c. 45.7 %
  - d. 68.2 %
7. ANOVA is an acronym for
  - a. Algebraic Number Variation Analysis
  - b. Alternative Numeric Variance Analysis
  - c. Analysis of Variance
  - d. Action Notation of Variation
8. The null hypothesis of an ANOVA is
  - a. All the treatment will give different results.
  - b. All the treatments will yield the same results.
  - c. The F ratio will equal 1.
  - d. The F ratio will be less than 1.
9. A factor tested at two levels has how many degrees of freedom?
  - a. 2
  - b. 0
  - c. 1
  - d. 3

10. What is the error term degrees of freedom for a  $2^3$  test with 3 replications?
- 16
  - 24
  - 8
  - 4
11. A  $2^3$  test with 3 replications indicates a contrast of 16.7 for factor A. What is the Sum of Squares for factor A?
- 16.7
  - 2.0875
  - 11.62
  - Not enough information.
12. The mean squares for factor A above is
- 16.7
  - 2.0875
  - 11.62
  - Not enough information.
13. A calculated probability for a factor or interaction of 0.05 indicates
- A 5% probability of the factor changing the test response.
  - A 5% probability of the result occurring randomly.
  - A 5% chance of success.
  - A 5 % chance of interaction.
14. The Total Sum of Squares for a  $2^3$  test with 2 replications and a standard deviation on all data of 15.8 is
- 3744.6
  - 237
  - 16.64
  - 1.05
15. A normal probability plot of residuals resulting in a straight line indicates a normal distribution and aids in validating the test data.
- True
  - False

A test of vibration levels in a milling process is proposed to test bit size, RPM and feed rate with the objective to minimize the vibration level. The factors are as follows:

	A: Bit Diameter	B : RPM	C: Feed Rate in/min
-	1/8	250	2
+	1/4	400	3.5

3 replications are run for each test with the data as follows:

Treatment	REP 1	REP 2	REP 3
1	25.025	17.7375	22.75
2	37.4	30.8	34
3	21.8625	20.7625	19.875

4	56.375	49.9125	51.25
5	25.9875	19.8	23.625
6	33	30.9375	30
7	19.9375	19.525	18.125
8	60.3625	54.8625	54.875

Use the 2 x3 template to fill in the data and perform the calculations for the answers to questions 16-xx.

16. What factors and interactions are calculated to be Statistically Significant at the 95% confidence level?
  - a. Bit Diameter and Feed Rate
  - b. Bit Diameter and RPM
  - c. Bit Diameter, RPM, Bit Diameter and RPM Interaction, Bit Diameter and RPM and Feed Rate Interaction.
  - d. Bit Diameter, Feed Rate, RPM and Feed Rate Interaction
17. The largest effect calculated is for
  - a. Bit Diameter
  - b. RPM
  - c. Feed Rate
  - d. Bit Diameter and RPM Interaction
18. Treatment 4 conditions are
  - a. 1/8 Bit Diameter, 250 RPM and 2 in/min feed rate
  - b. 1/4 Bit Diameter, 250 RPM and 3.5 in/min feed rate
  - c. 1/8 Bit Diameter, 400 RPM and 2 in/min feed rate
  - d. 1/4 Bit Diameter, 400 RPM and 2 in/min feed rate
19. The error Mean Squares is
  - a. 120.98
  - b. 7.56
  - c. 4634.3
  - d. 16
20. The lowest resulting vibration would be expected to be
  - a. 1/8 Bit Diameter, 250 RPM and 2 in/min feed rate
  - b. 1/4 Bit Diameter, 250 RPM and 3.5 in/min feed rate
  - c. 1/8 Bit Diameter, 250 RPM and 3.5 in/min feed rate
  - d. 1/4 Bit Diameter, 400 RPM and 3.5 in/min feed rate
21. The Signal to Noise Ratio for the Bit Diameter / RPM interaction is
  - a. 892
  - b. 38.5
  - c. 118
  - d. 12.2
22. The cumulative probability point (Pk) for the residual of treatment 5, rep 1 is
  - a. .604
  - b. .062
  - c. .479
  - d. .813

23. The rank of residual for treatment 4, rep 2 is
- a. 22
  - b. 4
  - c. 2
  - d. 1
24. The residuals plot for this test is a roughly linear line and indicates a normal distribution
- a. True
  - b. False
25. The mean value for vibration with a  $\frac{1}{4}$  diameter bit, 400 RPM and 3.5 in/min feed rate is
- a. 33.7
  - b. 56.7
  - c. 21.8
  - d. 31.2